

# SBMLDock

Docker Driven Systems Biology Tool Development and Usage

E. Z. Gnimpieba, M. Thavappiragasam, A. Chango, B. Conn,  
C. M. Lushbough

# Introduction

---

- Simplify researchers workflows
- Docker is a new emerging technology
- Work with our SBML tools

# SBMLDock

- Collects 7 CLI tools to manipulate SBML files
- We packaged in a special way
  - Each tool has it's needed libraries
  - We wrap java execution of all tools
  - We provide test data for each tool

# Tool specifics

---

- ParaABioS
- SBMLChecker
- SBMLCompare
- SBMLMerge



# Tool specifics

---

- SBMLSplit
- SBMLModeler
- SBMLAnnotate

# Docker specifics

---

- A self contained system
- Interacts with the kernel of the host system
- Repeatable and shareable
- Runs on Linux
  - Windows and Mac can work

# Docker specifics

- Mount volumes in the container

`-v /tmp/sbmldock:/tmp`

- Tell the container where to run

`-w /tmp`

- Run our image
- Call one of our programs

# Run a tool

- We've included test data
- This is what SBMLAnnotate would produce

```
wjconn@ted:/tmp/sbmldock$ docker run -v /tmp/sbmldock:/tmp -w /tmp usdbioinformatics/sbmldock SBMLAnnotate /opt/SBMLAnnotate/one.xml out.xml
start..
wjconn@ted:/tmp/sbmldock$ ls
hsperfdata_root jsbml.log out.xml
wjconn@ted:/tmp/sbmldock$
```

# Tools in a docker container

---

- Tools run the same on every system
- Docker images have unique numeric ids
- Containers run the same every time you start them

# Conclusion

---

- Collected SBML specific tools
- Docker provides:
  - Usability
  - Reproducibility
  - Unique identification

- **Acknowledgement:** This work has been partially supported by the National Science Foundation/EPSCoR Award No. IIA-1355423 and by the state of South Dakota, through BioSNTR.
- **References.**
- 1. Beasley, J.M., Coronado, G.D., Livaudais, J., Angeles-Llerenas, A., Ortega-Olvera, C., Romieu, I., Lazcano-Ponce, E., Torres-Mejía, G.: Alcohol and risk of breast cancer in Mexican women. *Cancer Causes Control.* 21, 863–870 (2010).
- 2. Cock, P.J.A., Grüning, B.A., Paszkiewicz, K., Pritchard, L.: Galaxy tools and workflows for sequence analysis with applications in molecular plant pathology. *PeerJ.* 1, e167 (2013).
- 3. Hucka, M.: Systems Biology Markup Language (SBML). In: Dubitzky, W., Wolkenhauer, O., Cho, K.-H., and Yokota, H. (eds.) *Encyclopedia of Systems Biology* SE - 1091. pp. 2057–2063. Springer New York (2013).
- 4. Thavappiragasam, M., Lushbough, C.M., Gnimpieba, E.Z.: Heuristic parallelizable algorithm for similarity based biosystems comparison. In: *Proceedings of the 5th ACM Conference on Bioinformatics, Computational Biology, and Health Informatics - BCB '14.* pp. 782–789 (2014).
- 5. Thavappiragasam, M., Lushbough, C., Gnimpieba, E.: SBMLChecker, a Semantic approach for SBML model reliability evaluation. *worldcomp-proceedings.com.* 2–5 (2014).
- 6. Thavappiragasam, M., Lushbough, C.M., Gnimpieba, E.Z.: Automatic biosystems comparison using semantic and name similarity. In: *Proceedings of the 5th ACM Conference on Bioinformatics, Computational Biology, and Health Informatics - BCB '14.* pp. 790–796 (2014).
- 7. Dräger, A., Rodriguez, N., Dumousseau, M., Dörr, A., Wrzodek, C., Le Novère, N., Zell, A., Hucka, M.: JSBML: a flexible Java library for working with SBML. *Bioinformatics.* 27, 2167–8 (2011).

***Opinion Paper***  
Evolutionary Constraint-Based  
Formulation Requires  
New Bi-level Solving Techniques

Marko Budinich, Jérémie Bourdon, Abdelhalim Larhlimi, Damien Eveillard  
**ComBi** Team, LINA, UMR 6241 CNRS, EMN, Université de Nantes



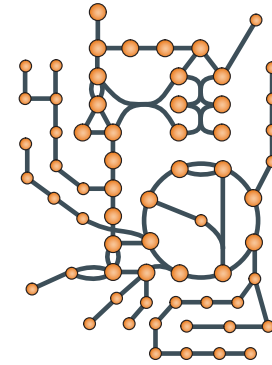
# Constraint Based Models

# Constraint Based Models

- Constraint Based Models are a type of metabolic models

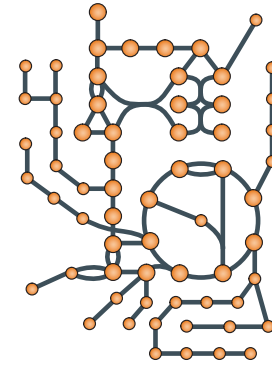
# Constraint Based Models

- Constraint Based Models are a type of metabolic models



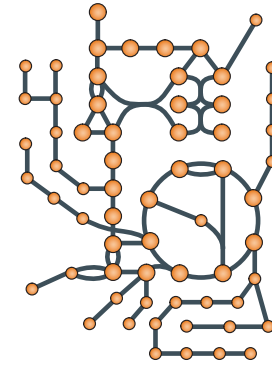
# Constraint Based Models

- Constraint Based Models are a type of metabolic models
- We are interested into rates of reactions  $\mathbf{v}$  (fluxes)



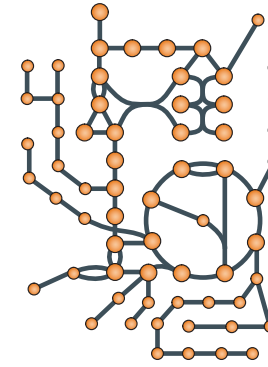
# Constraint Based Models

- Constraint Based Models are a type of metabolic models
- We are interested into rates of reactions  $\mathbf{v}$  (fluxes)
- Metabolic network is translated to a Stoichiometric Matrix



# Constraint Based Models

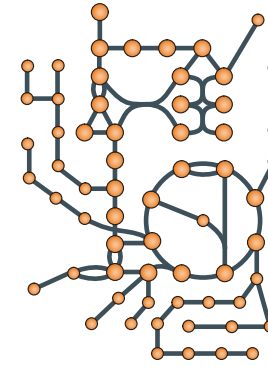
- Constraint Based Models are a type of metabolic models
- We are interested into rates of reactions  $\mathbf{v}$  (fluxes)
- Metabolic network is translated to a Stoichiometric Matrix



|             |           |    |    |    |    |   |   |   |    |
|-------------|-----------|----|----|----|----|---|---|---|----|
| Metabolites | -1        | 0  | 0  | 0  | 0  | 1 | 0 | 0 | 0  |
|             | -1        | 0  | 0  | 0  | 0  | 0 | 1 | 0 | 0  |
|             | 0         | 0  | 0  | -1 | -1 | 0 | 0 | 1 | 0  |
|             | 1         | -1 | 0  | 1  | 0  | 0 | 0 | 0 | 0  |
|             | 0         | 1  | -1 | 0  | 0  | 0 | 0 | 0 | 0  |
|             | 0         | 0  | -1 | 0  | 1  | 0 | 0 | 0 | 0  |
|             | 0         | 0  | 1  | 0  | 0  | 0 | 0 | 0 | -1 |
|             | Reactions |    |    |    |    |   |   |   |    |

# Constraint Based Models

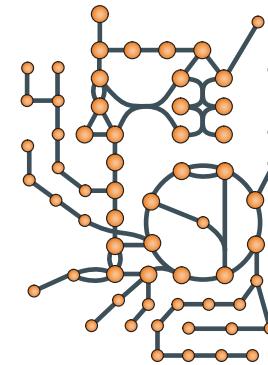
- Constraint Based Models are a type of metabolic models
- We are interested into rates of reactions  $\mathbf{v}$  (fluxes)
- Metabolic network is translated to a Stoichiometric Matrix
- Steady State Mass Balance and bound constraints defines a solution space



|             |           |    |    |    |    |   |   |   |    |
|-------------|-----------|----|----|----|----|---|---|---|----|
| Metabolites | -1        | 0  | 0  | 0  | 0  | 1 | 0 | 0 | 0  |
|             | -1        | 0  | 0  | 0  | 0  | 0 | 1 | 0 | 0  |
|             | 0         | 0  | 0  | -1 | -1 | 0 | 0 | 1 | 0  |
|             | 1         | -1 | 0  | 1  | 0  | 0 | 0 | 0 | 0  |
|             | 0         | 1  | -1 | 0  | 0  | 0 | 0 | 0 | 0  |
|             | 0         | 0  | -1 | 0  | 1  | 0 | 0 | 0 | 0  |
|             | 0         | 0  | 1  | 0  | 0  | 0 | 0 | 0 | -1 |
|             | Reactions |    |    |    |    |   |   |   |    |

# Constraint Based Models

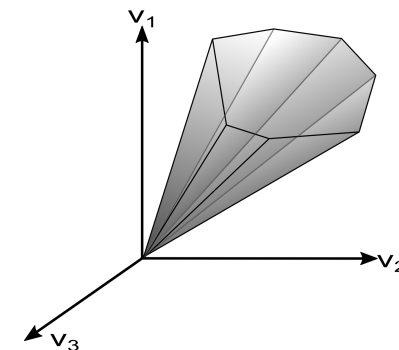
- Constraint Based Models are a type of metabolic models
- We are interested into rates of reactions  $\mathbf{v}$  (fluxes)
- Metabolic network is translated to a Stoichiometric Matrix
- Steady State Mass Balance and bound constraints defines a solution space



|             |           |    |    |    |    |   |   |   |    |
|-------------|-----------|----|----|----|----|---|---|---|----|
|             | -1        | 0  | 0  | 0  | 0  | 1 | 0 | 0 | 0  |
|             | -1        | 0  | 0  | 0  | 0  | 0 | 1 | 0 | 0  |
| Metabolites | 0         | 0  | 0  | -1 | -1 | 0 | 0 | 1 | 0  |
|             | 1         | -1 | 0  | 1  | 0  | 0 | 0 | 0 | 0  |
|             | 0         | 1  | -1 | 0  | 0  | 0 | 0 | 0 | 0  |
|             | 0         | 0  | -1 | 0  | 1  | 0 | 0 | 0 | 0  |
|             | 0         | 0  | 1  | 0  | 0  | 0 | 0 | 0 | -1 |
|             | Reactions |    |    |    |    |   |   |   |    |

$$\frac{d[\mathbf{C}]}{dt} = \mathbf{S}\mathbf{v} = 0$$

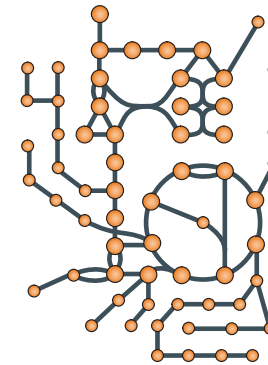
$$\mathbf{lb} \leq \mathbf{v} \leq \mathbf{ub}$$





# Constraint Based Models

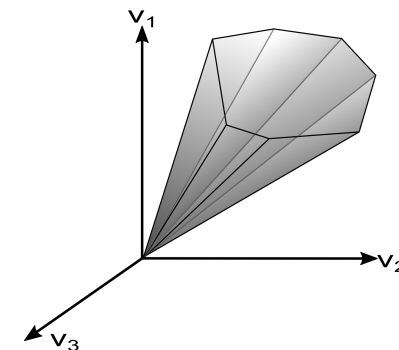
- Constraint Based Models are a type of metabolic models
- We are interested into rates of reactions  $\mathbf{v}$  (fluxes)
- Metabolic network is translated to a Stoichiometric Matrix
- Steady State Mass Balance and bound constraints defines a solution space
- Usually formalized as optimization problem



|             |    |    |    |    |    |   |   |   |    |
|-------------|----|----|----|----|----|---|---|---|----|
| Metabolites | -1 | 0  | 0  | 0  | 0  | 1 | 0 | 0 | 0  |
|             | -1 | 0  | 0  | 0  | 0  | 0 | 1 | 0 | 0  |
|             | 0  | 0  | 0  | -1 | -1 | 0 | 0 | 1 | 0  |
|             | 1  | -1 | 0  | 1  | 0  | 0 | 0 | 0 | 0  |
|             | 0  | 1  | -1 | 0  | 0  | 0 | 0 | 0 | 0  |
|             | 0  | 0  | -1 | 0  | 1  | 0 | 0 | 0 | 0  |
|             | 0  | 0  | 1  | 0  | 0  | 0 | 0 | 0 | -1 |
| Reactions   |    |    |    |    |    |   |   |   |    |

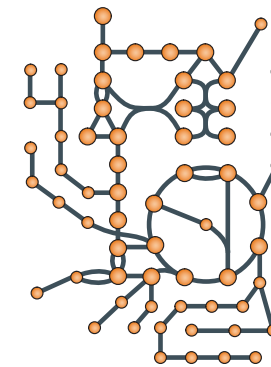
$$\frac{d[\mathbf{C}]}{dt} = \mathbf{S}\mathbf{v} = 0$$

$$\mathbf{lb} \leq \mathbf{v} \leq \mathbf{ub}$$



# Constraint Based Models

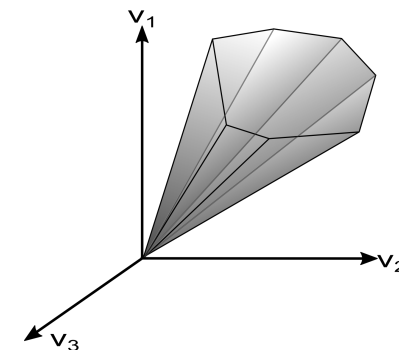
- Constraint Based Models are a type of metabolic models
- We are interested into rates of reactions  $\mathbf{v}$  (fluxes)
- Metabolic network is translated to a Stoichiometric Matrix
- Steady State Mass Balance and bound constraints defines a solution space
- Usually formalized as optimization problem



|             |           |    |    |    |    |   |   |   |    |
|-------------|-----------|----|----|----|----|---|---|---|----|
|             | -1        | 0  | 0  | 0  | 0  | 1 | 0 | 0 | 0  |
|             | -1        | 0  | 0  | 0  | 0  | 0 | 1 | 0 | 0  |
| Metabolites | 0         | 0  | 0  | -1 | -1 | 0 | 0 | 1 | 0  |
|             | 1         | -1 | 0  | 1  | 0  | 0 | 0 | 0 | 0  |
|             | 0         | 1  | -1 | 0  | 0  | 0 | 0 | 0 | 0  |
|             | 0         | 0  | -1 | 0  | 1  | 0 | 0 | 0 | 0  |
|             | 0         | 0  | 1  | 0  | 0  | 0 | 0 | 0 | -1 |
|             | Reactions |    |    |    |    |   |   |   |    |

$$\frac{d[\mathbf{C}]}{dt} = \mathbf{S}\mathbf{v} = 0$$

$$\mathbf{lb} \leq \mathbf{v} \leq \mathbf{ub}$$



$$\max \mathbf{c}^T \mathbf{v}$$

s.t

$$\mathbf{S}\mathbf{v} = 0$$

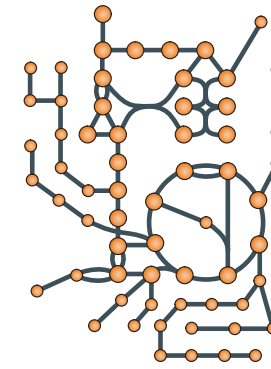
$$\mathbf{lb} \leq \mathbf{v} \leq \mathbf{ub}$$

$$\mathbf{v}_i = \mathbf{E}, i \in \mathcal{L}$$

...

# Constraint Based Models

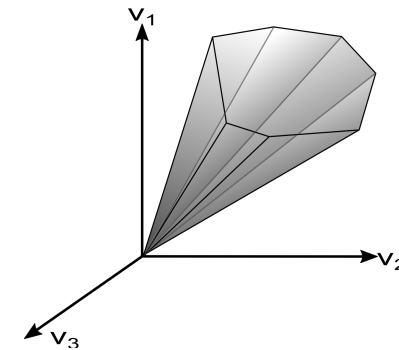
- Constraint Based Models are a type of metabolic models
- We are interested into rates of reactions  $\mathbf{v}$  (fluxes)
- Metabolic network is translated to a Stoichiometric Matrix
- Steady State Mass Balance and bound constraints defines a solution space
- Usually formalized as optimization problem



|             |    |    |    |    |    |   |   |   |    |
|-------------|----|----|----|----|----|---|---|---|----|
| Metabolites | -1 | 0  | 0  | 0  | 0  | 1 | 0 | 0 | 0  |
|             | -1 | 0  | 0  | 0  | 0  | 0 | 1 | 0 | 0  |
|             | 0  | 0  | 0  | -1 | -1 | 0 | 0 | 1 | 0  |
|             | 1  | -1 | 0  | 1  | 0  | 0 | 0 | 0 | 0  |
|             | 0  | 1  | -1 | 0  | 0  | 0 | 0 | 0 | 0  |
|             | 0  | 0  | -1 | 0  | 1  | 0 | 0 | 0 | 0  |
|             | 0  | 0  | 1  | 0  | 0  | 0 | 0 | 0 | -1 |
| Reactions   |    |    |    |    |    |   |   |   |    |

$$\frac{d[\mathbf{C}]}{dt} = \mathbf{S}\mathbf{v} = 0$$

$$\mathbf{lb} \leq \mathbf{v} \leq \mathbf{ub}$$



$$\max \mathbf{c}^T \mathbf{v}$$

s.t

$$\mathbf{S}\mathbf{v} = 0$$

$$\mathbf{lb} \leq \mathbf{v} \leq \mathbf{ub}$$

$$\mathbf{v}_i = \mathbf{E}, i \in \mathcal{L}$$

...

# Evolution

# Evolution

## A NEW EVOLUTIONARY LAW

Leigh Van Valen  
Department of Biology  
The University of Chicago  
Chicago, Illinois 60637

### ABSTRACT:

All groups for which data exist go extinct at a rate that is constant for a given group. When this is recast in ecological form (the effective environment of any homogeneous group of organisms deteriorates at a stochastically constant rate), no definite exceptions exist although a few are possible. Extinction rates are similar within some very broad categories and vary regularly with size of area inhabited. A new unit of rates for discrete phenomena, the macarthur, is introduced. Laws are appropriate in evolutionary

# Evolution

## A NEW EVOLUTIONARY LAW

Leigh Van Valen  
Department of Biology  
The University of Chicago  
Chicago, Illinois 60637

### ABSTRACT:

All groups for which data exist go extinct at a rate that is a given group. When this is recast in ecological form (the effectually constant rate), no definite exceptions exist although a few. Extinction rates are similar within some very broad categories and vary regularly with size of area inhabited. A new unit of rates for discrete phenomena, the macarthur, is introduced. Laws are appropriate in evolutionary



# Evolution

## A NEW EVOLUTIONARY LAW

Leigh Van Valen  
Department of Biology  
The University of Chicago  
Chicago, Illinois 60637

### ABSTRACT:

All groups for which data exist go extinct at a rate that is a given group. When this is recast in ecological form (the effectually constant rate), no definite exceptions exist although a few extinction rates are similar within some very broad categories and vary regularly with size of area inhabited. A new unit of rates for discrete phenomena, the macarthur, is introduced. Laws are appropriate evolutionary



### OPINION/HYPOTHESIS

## The Black Queen Hypothesis: Evolution of Dependencies through Adaptive Gene Loss

J. Jeffrey Morris,<sup>a,b</sup> Richard E. Lenski,<sup>a,b</sup> and Erik R. Zinser<sup>c</sup>  
<sup>a</sup>Michigan State University, East Lansing, Michigan, USA<sup>a</sup>; <sup>b</sup>BEACON Center for the Study of Evolution in Action, East Lansing, Michigan, USA<sup>b</sup>; and <sup>c</sup>University of Tennessee, Knoxville, Tennessee, USA<sup>c</sup>



# Evolution

## A NEW EVOLUTIONARY LAW

Leigh Van Valen  
Department of Biology  
The University of Chicago  
Chicago, Illinois 60637



### ABSTRACT:

All groups for which data exist go extinct at a rate that is environmentally constant. When this is recast in ecological form (the effectually constant rate), no definite exceptions exist although a few extinction rates are similar within some very broad categories and vary regularly with size of area inhabited. A new unit of rates for discrete phenomena, the macarthur, is introduced. Laws are appropriate for evolutionary

### OPINION/HYPOTHESIS

## The Black Queen Hypothesis: Evolution of Dependencies through Adaptive Gene Loss

J. Jeffrey Morris,<sup>a,b</sup> Richard E. Lenski,<sup>a,b</sup> and Erik R. Zinser<sup>c</sup>  
<sup>a</sup>Michigan State University, East Lansing, Michigan, USA<sup>a</sup>; <sup>b</sup>BEACON Center for the Study of Evolution in Action, East Lansing, Michigan, USA<sup>b</sup>; and <sup>c</sup>Knoxville, Tennessee, USA<sup>c</sup>





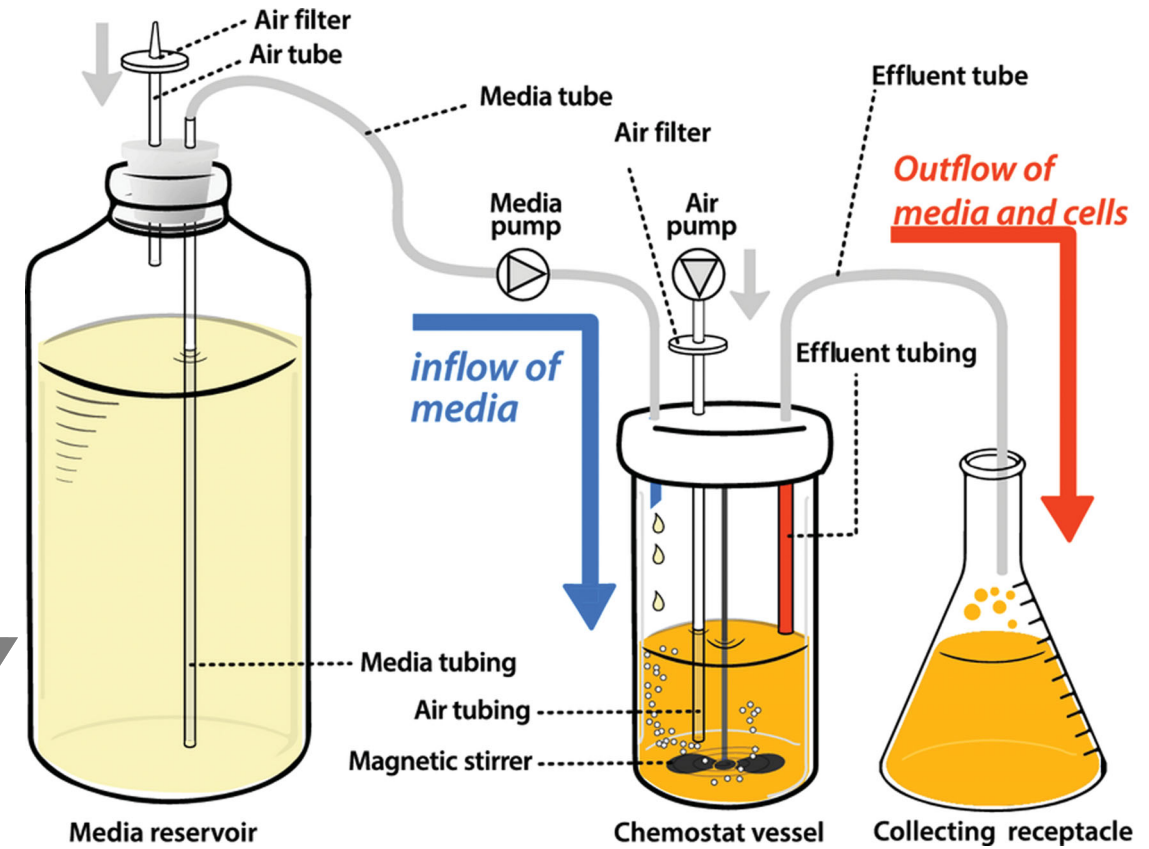
# Evolution

## A NEW EVOLUTIONARY LAW

Leigh Van Valen  
Department of Biology  
The University of Chicago  
Chicago, Illinois 60637

### ABSTRACT:

All groups for which data exist go extinct at a rate that is environmentally constant. When this is recast in ecological form (the effectually constant rate), no definite exceptions exist although a few regularly with size of area inhabited. A new unit of rates for discrete phenomena, the *macarthur*, is introduced. Laws are appropriate for evolutionary



### OPINION/HYPOTHESIS

## The Black Queen Hypothesis: Evolution of Dependencies through Adaptive Gene Loss

J. Jeffrey Morris,<sup>a,b</sup> Richard E. Lenski,<sup>a,b</sup> and Erik R. Zinser  
Michigan State University, East Lansing, Michigan, USA<sup>a</sup>; BEACON Center for the Study of Evolution in Action, East Lansing, Michigan, USA<sup>b</sup>; and  
Knoxville, Tennessee, USA<sup>c</sup>

# Evolution

## ABSTRACT:

All groups for which data exist go extinct at a rate that is a given group. When this is recast in ecological form (the effectually constant rate), no definite exceptions exist although a few extinction rates are similar within some very broad categories and vary regularly with size of area inhabited. A new unit of rates for discrete phenomena, the *macarthur*, is introduced. Laws are appropriate for evolutionary

## A NEW EVOLUTIONARY LAW

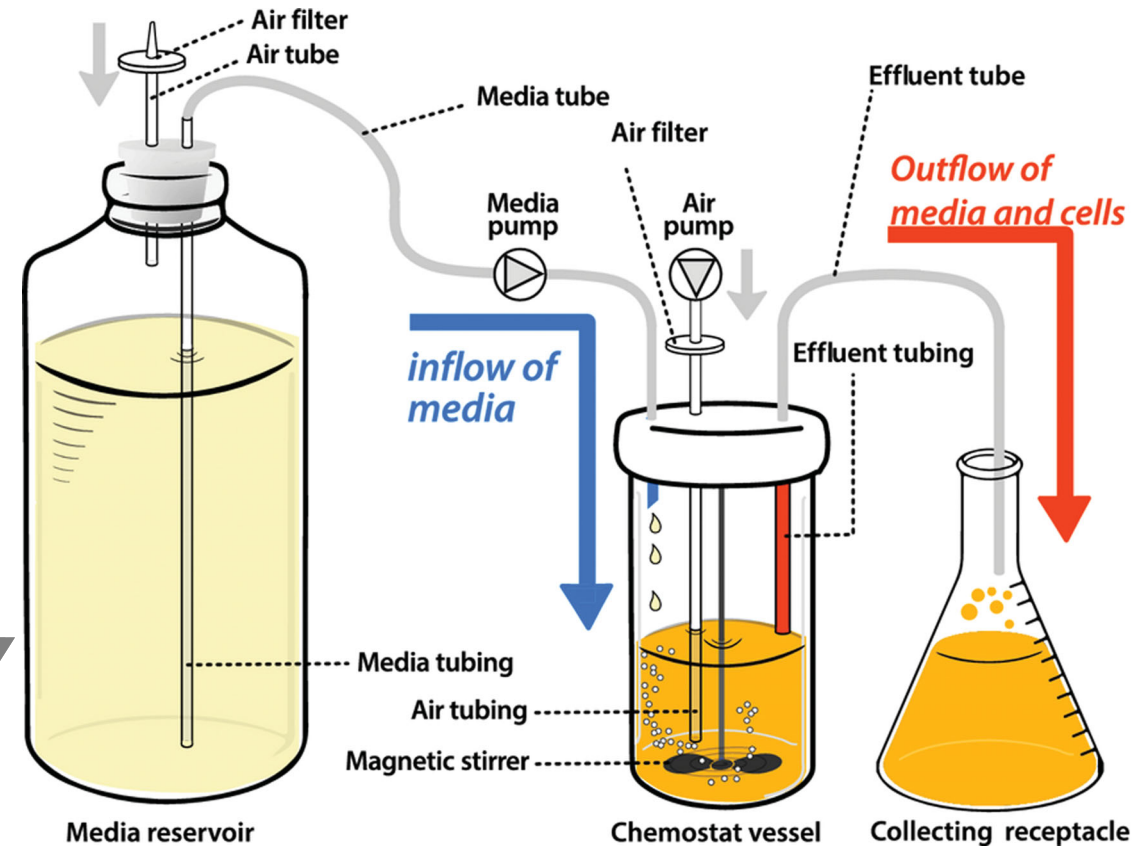
Leigh Van Valen  
Department of Biology  
The University of Chicago  
Chicago, Illinois 60637



## OPINION/HYPOTHESIS

## The Black Queen Hypothesis: Evolution of Dependencies through Adaptive Gene Loss

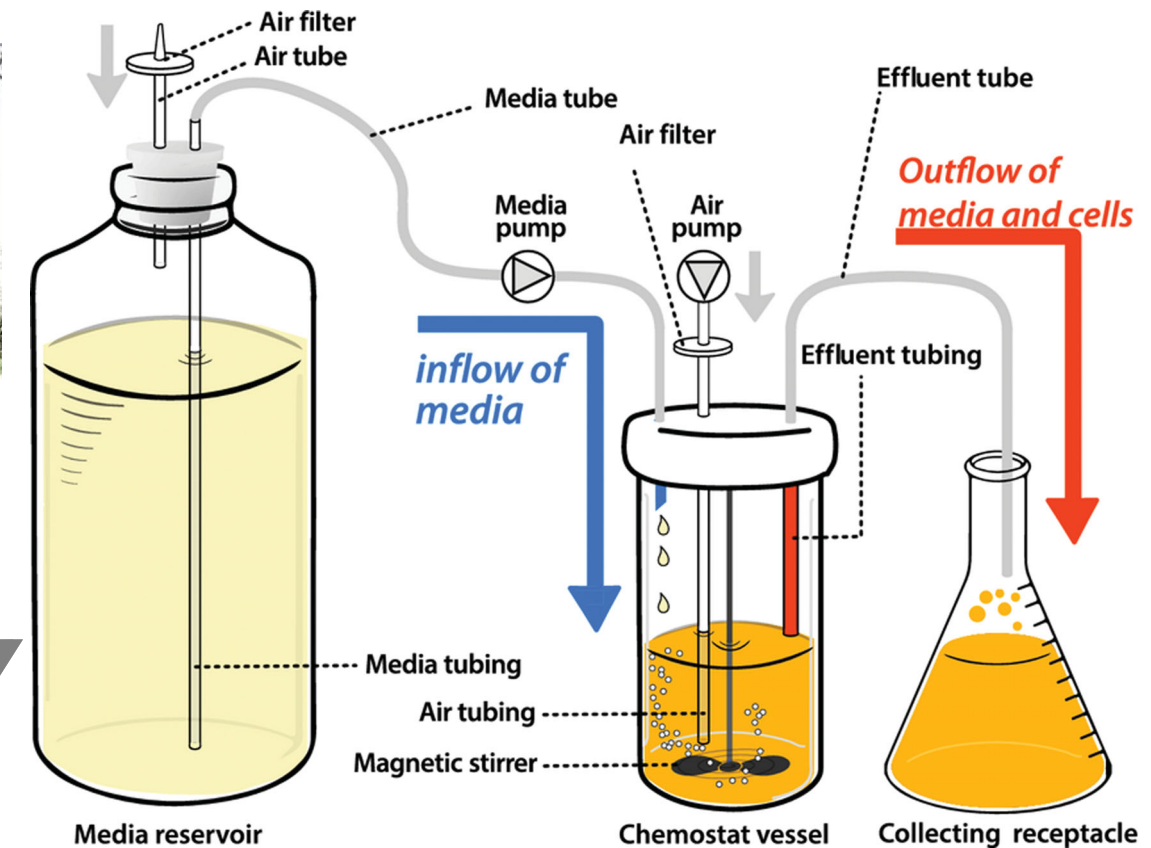
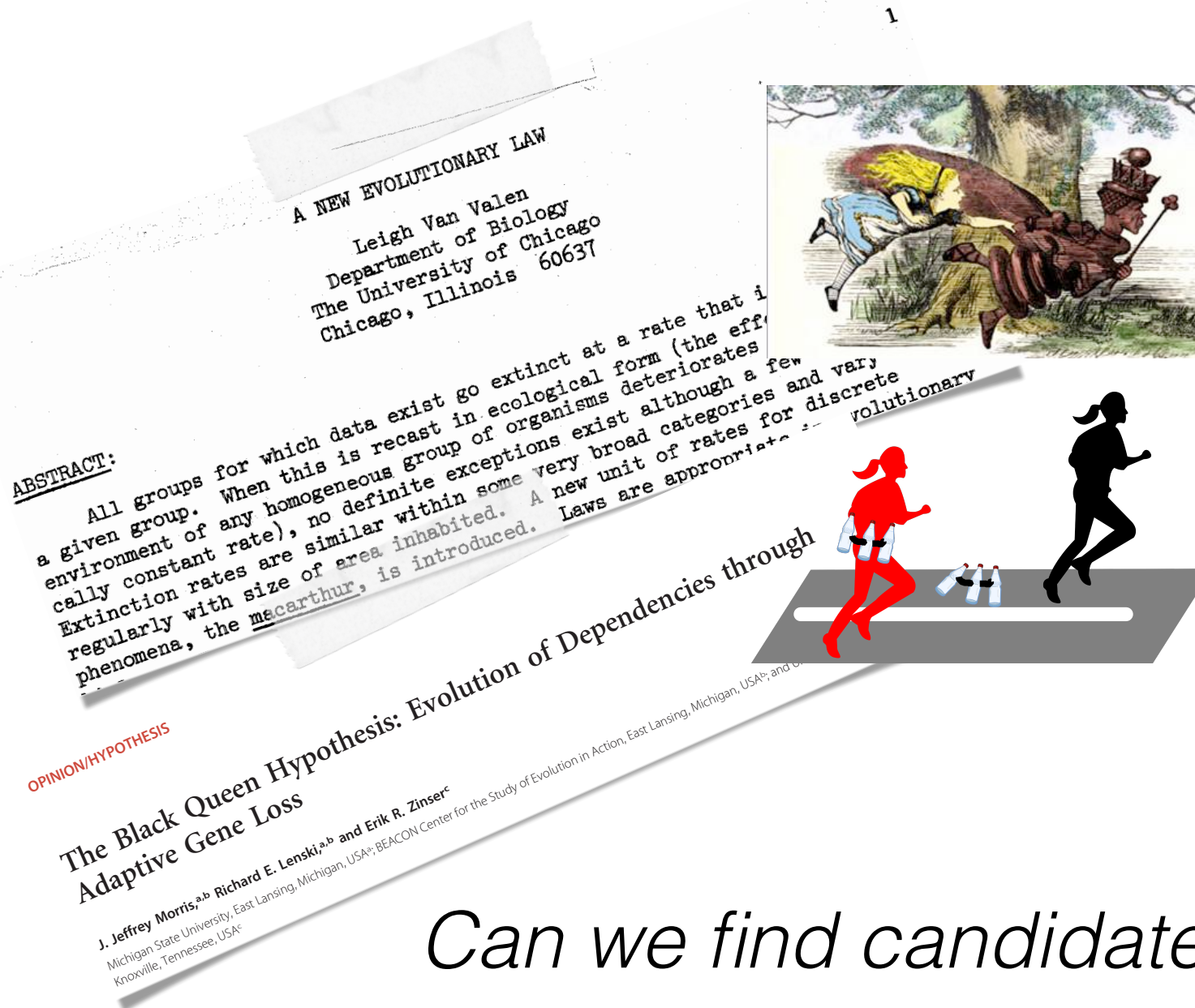
J. Jeffrey Morris,<sup>a,b</sup> Richard E. Lenski,<sup>a,b</sup> and Erik R. Zinser<sup>c</sup>  
<sup>a</sup>Michigan State University, East Lansing, Michigan, USA<sup>a</sup>; <sup>b</sup>BEACON Center for the Study of Evolution in Action, East Lansing, Michigan, USA<sup>b</sup>; and <sup>c</sup>Knoxville, Tennessee, USA<sup>c</sup>



*Can we find candidate genes for these theories?*



# Evolution



*Can we find candidate genes for these theories?*

Van Valen, L. (1973). A new evolutionary law. *Evolutionary Theory*, 1, 1–30.

Van Valen, L. (1974). Molecular evolution as predicted by natural selection. *Journal of Molecular Evolution*, 3(2), 89–101.

Morris, J. J., Lenski, R. E., & Zinser, E. R. (2012). The Black Queen Hypothesis: evolution of dependencies through adaptive gene loss. *mBio*, 3(2)

Gresham, D., & Hong, J. (2014). The functional basis of adaptive evolution in chemostats. *Fems Microbiology Reviews*

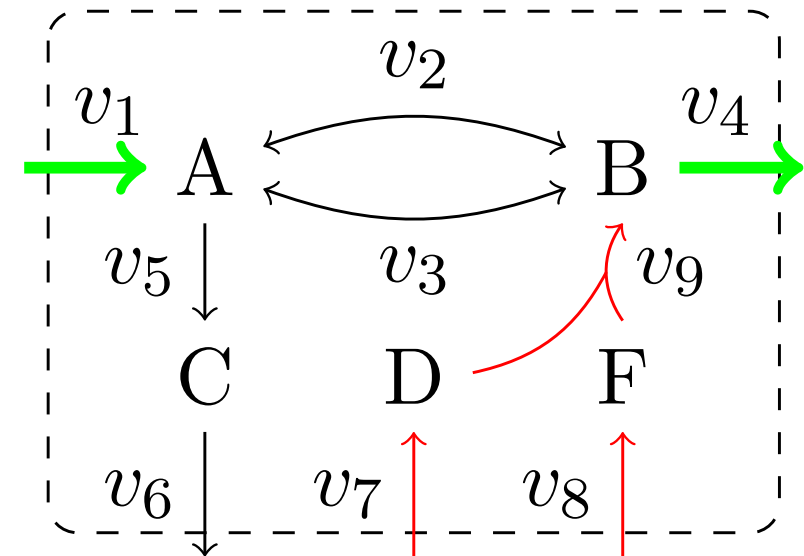
# Gene Loss using CBM

# Gene Loss using CBM

- Blocked reactions are reactions that **can not** carry flux under given conditions

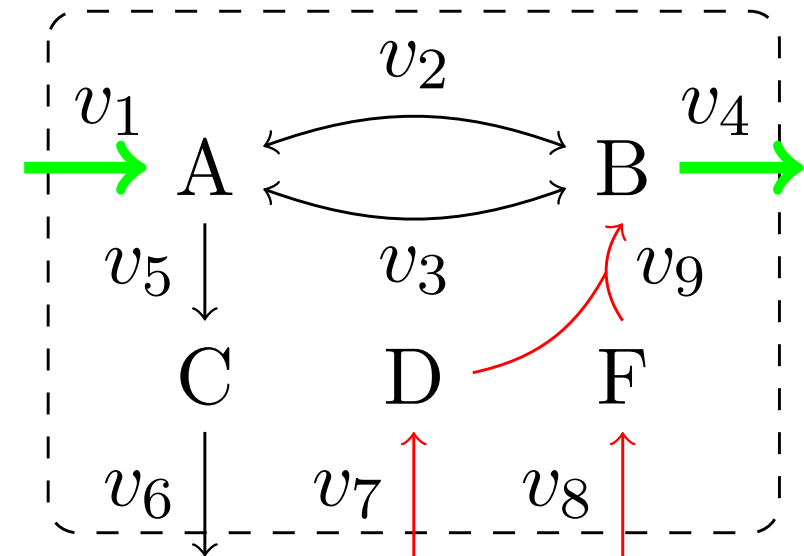
# Gene Loss using CBM

- Blocked reactions are reactions that **can not** carry flux under given conditions



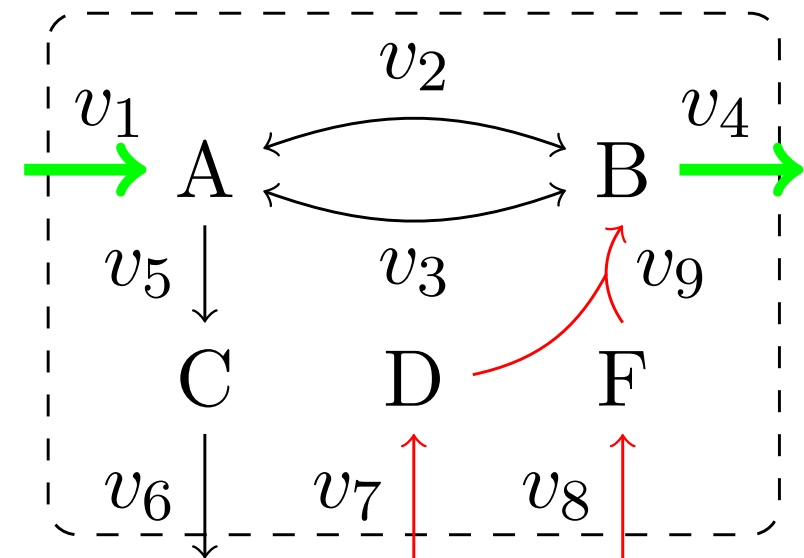
# Gene Loss using CBM

- Blocked reactions are reactions that **can not** carry flux under given conditions
- We expect that these reactions will be loosed through evolution



# Gene Loss using CBM

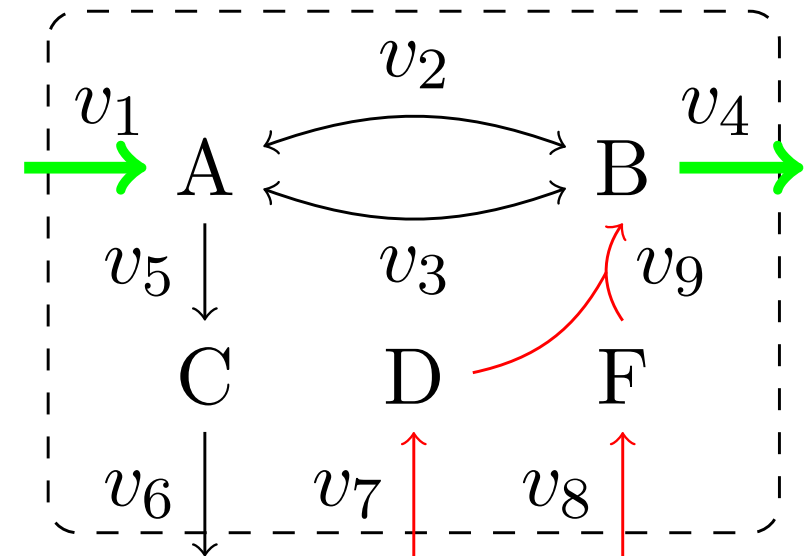
- Blocked reactions are reactions that **can not** carry flux under given conditions
- We expect that these reactions will be loosed through evolution
- Given a set of conditions **E**, we can find blocked reactions through simulation





# Gene Loss using CBM

- Blocked reactions are reactions that **can not** carry flux under given conditions
- We expect that these reactions will be loosed through evolution
- Given a set of conditions  $\mathbf{E}$ , we can find blocked reactions through simulation



$$\max \mathbf{c}^T \mathbf{v}$$

s.t

$$\mathbf{S}\mathbf{v}=\mathbf{0}$$

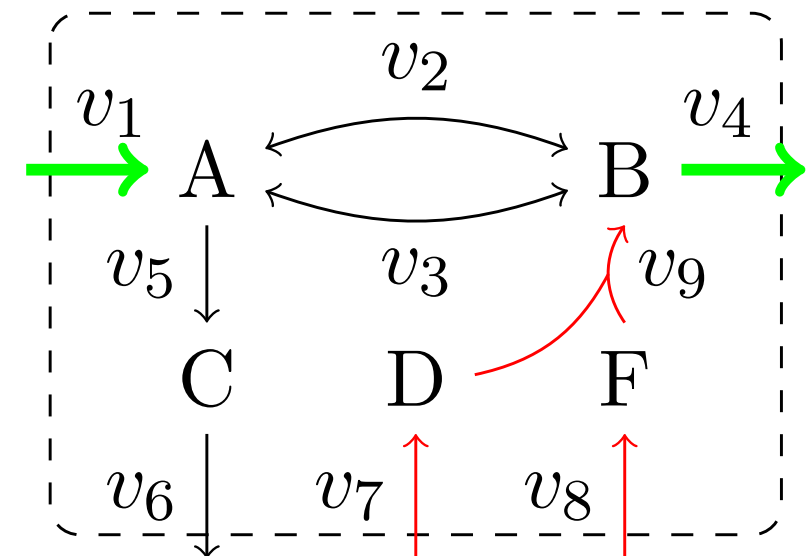
$$\mathbf{lb} \leq \mathbf{v} \leq \mathbf{ub}$$

$$\mathbf{v}_i = \mathbf{E}_i, i \in \mathcal{L}$$

...

# Gene Loss using CBM

- Blocked reactions are reactions that **can not** carry flux under given conditions
- We expect that these reactions will be loosed through evolution
- Given a set of conditions **E**, we can find blocked reactions through simulation



$$\max c^T v$$

s.t

$$Sv=0$$

$$lb \leq v \leq ub$$

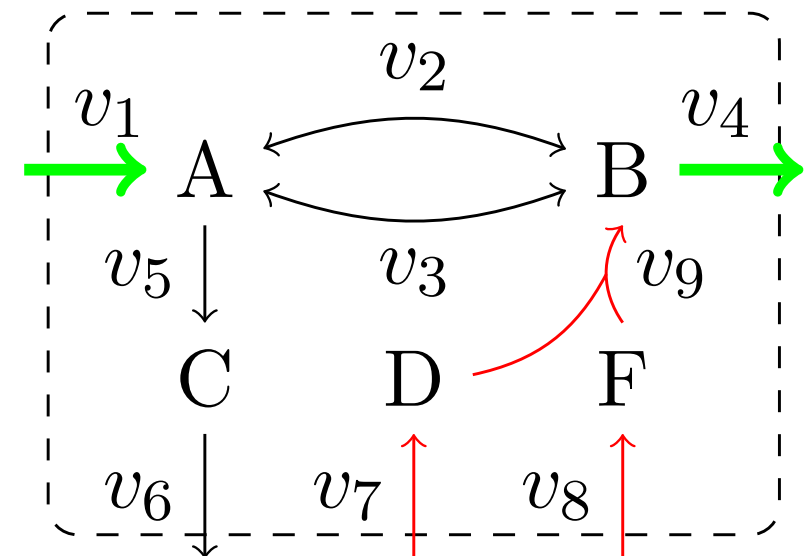
...

$$v_i = E_i, i \in \mathcal{L}$$

...

# Gene Loss using CBM

- Blocked reactions are reactions that **can not** carry flux under given conditions
- We expect that these reactions will be loosed through evolution
- Given a set of conditions  $\mathbf{E}$ , we can find blocked reactions through simulation



$$\max c^T v$$

s.t

$$Sv=0$$

$$lb \leq v \leq ub$$

$$v_i = \mathbf{E}_1, i \in \mathcal{L}$$

...

$$\max c^T v$$

s.t

$$Sv=0$$

$$lb \leq v \leq ub$$

$$v_i = \mathbf{E}_n, i \in \mathcal{L}$$

...

It is possible to determine  
conditions **E** to obtain most of  
blocked reactions?

# A Bi-Level Optimization Approach

# A Bi-Level Optimization Approach

First, we find number of  
blocked reactions

# A Bi-Level Optimization Approach

First, we find number of blocked reactions

$$\max \sum_{i=1}^n f_i^+ + f_i^-$$

subject to

$$\mathbf{S}\mathbf{v} = 0 \quad (1)$$

$$\mathbf{lb} \leq \mathbf{v} \leq \mathbf{ub} \quad (2)$$

$$\mathbf{v}_L = \mathbf{E}, \quad L \in \mathcal{L} \quad (3)$$

$$f_i^+, f_i^- \in \{0, 1\} \quad (4)$$

$$f_i^+ + f_i^- \leq 1 \quad (5)$$

$$v_i \geq \epsilon f_i^+ - M f_i^- \quad (6)$$

$$v_i \leq -\epsilon f_i^- + M f_i^+ \quad (7)$$

# A Bi-Level Optimization Approach

First, we find number of blocked reactions

$$\max \sum_{i=1}^n f_i^+ + f_i^-$$

subject to

$$\mathbf{S}\mathbf{v} = 0 \quad (1)$$

$$\mathbf{lb} \leq \mathbf{v} \leq \mathbf{ub} \quad (2)$$

$$\mathbf{v}_L = \mathbf{E}, \quad L \in \mathcal{L} \quad (3)$$

$$f_i^+, f_i^- \in \{0, 1\} \quad (4)$$

$$f_i^+ + f_i^- \leq 1 \quad (5)$$

$$v_i \geq \epsilon f_i^+ - M f_i^- \quad (6)$$

$$v_i \leq -\epsilon f_i^- + M f_i^+ \quad (7)$$

Next, we pick settings  $\mathbf{E}$  to maximize blocked reactions



# A Bi-Level Optimization Approach

First, we find number of blocked reactions

$$\max \sum_{i=1}^n f_i^+ + f_i^-$$

subject to

$$\mathbf{S}\mathbf{v} = 0 \quad (1)$$

$$\mathbf{lb} \leq \mathbf{v} \leq \mathbf{ub} \quad (2)$$

$$\mathbf{v}_L = \mathbf{E}, \quad L \in \mathcal{L} \quad (3)$$

$$f_i^+, f_i^- \in \{0, 1\} \quad (4)$$

$$f_i^+ + f_i^- \leq 1 \quad (5)$$

$$v_i \geq \epsilon f_i^+ - M f_i^- \quad (6)$$

$$v_i \leq -\epsilon f_i^- + M f_i^+ \quad (7)$$

Next, we pick settings  $\mathbf{E}$  to maximize blocked reactions

$$\min z$$

subject to

$$\mathbf{lb}_L \leq \mathbf{E} \leq \mathbf{ub}_L$$

$$z = \max \sum f_i^+ + f_i^-$$

subject to

$$\mathbf{S}\mathbf{v}=0 \quad (1)$$

$$\mathbf{lb} \leq \mathbf{v} \leq \mathbf{ub} \quad (2)$$

$$\mathbf{v}_L = \mathbf{E}, \quad L \in \mathcal{L} \quad (3)$$

$$\dots \quad \dots$$

$$v_i \leq -\epsilon f_i^- + M f_i^+ \quad (7)$$

# What is next?

- In general, Mixed Integer Bi-Level problems are considered as an “still unsolved”
- Links environmental conditions to evolution processes
- Developing algorithms to solve these type of problems are of interest in System Biology

*“Nothing in Biology Makes Sense Except in the  
Light of Evolution”*

– Theodosius Dobzhansky (1900-1975)

Thanks for your  
attention!